

Name : _____ R. No. _____ Class/ Sec: _____ Date: _____ Invig. Sign _____

ATOMIC ENERGY CENTRAL SCHOOL, NARORA
CLASS XII MATHEMATICS UNIT TEST FIRST 2018-19

MM: 50

TIME : 1:30 Hr.

General Instructions:

- All questions are compulsory and marks are mentioned in front of each question.
- Electronic devices are prohibited to use in the examination.
- Use Blue or Black Pen only.
- Question number 1 carry 2 marks, question number 2 to 4 are 4 marks each and Question number 5 to 10 are 6 marks each.

- 1 A matrix of order 3×3 has determinant 5, find $|3A|$
- 2 Find the interval in which function $f(x) = \sin x + \cos x$, $0 \leq x \leq 2\pi$ increasing or decreasing
- 3 If $y = \cos x^x$, find dy/dx
- 4 Using differential find the approximate value of $\sqrt{0.037}$
- 5 Prove that the relation R on Z of all integers defined by $(a, b) \in R$ if $(a - b)$ is divisible by 5 is an equivalence relation
- 6 Using properties of determinant prove that

$$(a-b)(b-c)(c-a)(a+b+c) = \begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$$
- 7 Find k , if $f(x) = \begin{cases} k \cos x & \text{if } x \neq \pi/2 \\ \pi - 2x & \text{if } x = \pi/2 \end{cases}$ is continuous at $x = \pi/2$
- 8 An open box, with a square base is to be made out of a given quantity of metal sheet of area c^2 . Show that the maximum volume is $c^3/6\sqrt{3}$
- 9 Using elementary transformation find the inverse of the matrix

$$\begin{bmatrix} 7 & 4 \\ 5 & 2 \end{bmatrix}$$
- 10 Show that the curves $2x = y^2$ and $2xy = k$ cut at right angle, if $k^2 = 8$